**Improved Correlation Coefficients of Fermatean Pentapartitioned single valued**

**neutrosophic sets and interval Fermatean Pentapartitioned neutrosophic**

**sets for multiple attribute decision making**

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**Abstract**:

A correlation coefficient is a statistical measure that helps identify how much changes in one value signal changes in another.Wang's single valued neutrosophic sets were improvised into Fermatean Pentapartitioned single valued neutrosophic sets. We have investigated and looked into the attributes of interval Fermatean Pentapartitioned neutrosophic sets and Fermatean Pentapartitioned single valued neutrosophic sets in this work. Additionally, we have used this idea in many decision-making techniques using interval and Fermatean pentapartitioned single valued neutrosophic environments. Eventually we presuming (that) an example using the problems of many attribute decision making that was previously suggested.

**Keywords:** Improved correlation coefficient, interval Fermatean Pentapartitioned neutrosophic sets, and Fermatean Pentapartitioned single valued neutrosophic sets are other related terms.

**Introduction:**

In 1965, Zadeh [21] developed fuzzy sets, a development of classical set theory that permits the membership function to be valued in the range [0, 1]. In 1986, Atanassov [1] presented the intuitionistic fuzzy set (IFS), a development of Zadhe's fuzzy set theory that entail the degree of membership and degree of non-membership and  the interval range is [0,1]. IFS theory is frequently used in disciplines like logic programming, problem-solving in decision-making, and medical diagnosis, among others.

In 1995, Florentin Smarandache [11] developed the basic thought of a neutrosphic set, which imparts skill of neutral thought by introducing a brand-new component known as indeterminacy to the set. The truth membership function (T), indeterminacy membership function (I), and falsity membership

function (F) were therefore included in the framing of the neutrosophic set. The non- standard interval [0, 1]

 is dealt with by neutrosophic sets. Neutrophic set to take part of vital role in many application fields.

 This is because it deals with Indeterminacy well.

Single valued nuetrosophic sets (SVNS), commonly known as an extension of intuitionistic fuzzy sets, were presented by Wang [12](2010), and they have since been a very hot area of research. The notion of Fermatean Pentapartitioned Single Valued Neutosophic Sets, which is placed on Belnap's Four Logic and Smarandache's Four Numerical Valued Logic, was proposed by Rajashi Chatterjee, et al. [10]. The (FPSVNS) has five components because the indeterminacy is split into the "Contradiction" (both true and false) and "unknown" (neither true nor false) functions: TA, CA, KA, UA, and FA, all of which fall inside the non-standard unit interval [0, 1].

The correlation coefficient is a helpful statistical tool for calculating how closely two variables are related to one another. The correlation of fuzzy sets under a fuzzy environment was proposed in 1999 by D.A. In this essay, part 2 provides some fundamental ideas of Fermatean pentapartitioned neutrosophic sets, quadripartitioned single valued neutrosophic sets, and their complements. It also talk over union, intersection, interval neutrosophic sets, and the correlation coefficient of FPSVNS. In part 3, we introduced the concept of improved correlation coefficient of FPSVNSs to handle the regulation of correlation coefficient as described. We also enclosed some of its properties and a decision-making approach using the improved correlation coefficient of FPSVNSs. Interval Fermatean Pentapartitioned Neutrosophic sets (IFPNS) were introduced in part 4 with some basic definitions and a determined correlation coefficient. Furthermore, we have talked about a part of its characteristics and a strategy for making decisions applying an environment with an interval Fermatean pentapartitioned neutrosophic. In part 5, an illustration likewise -planned correlation method in decision-making with many criteria is provided. The paper is concluded in part 6.

**2. Preliminaries:**

**2.1 Quadripartitioned single valued neutrosophic sets:**

Definition 2.1. [5]

The single valued neutrosophic sets, which are defined over the standard unit interval [0, 1], neutrosophic sets are expressed across the non-standard unit range [0, 1]. It refers that the definition of a single-valued

neutrosophic set A is x X}

where like that .

**Definition 2.2. [4]**

Let X be a set that is non-empty. A quadripartitioned single valued neutrosophic set (QSVNS) A over X characterizes each element in X by a truth membership function , a contradiction membership function , an ignorance membership function along with a falsity membership function like that x X, and whereupon X is discrete. R is act as

R =.

Definition 2.2. [15]

Let X be a universe. A Fermatean pentapartitioned neutrosophic set (FPN) R on X is

R = {< x, TA , CA , KA , UA , FA ,) >: x X } such that (TA)3 + (CA)3 + (KA)3+ (UA)3 + (FA)3 ≤ 3

Here, TA(x) is the truth membership,

CA(x) is contradiction membership,

KA(x) is ignorance membership,

UA (x) is unknown membership,

FA(x) is the false membership.

**3. Fermatean pentapartioned single valued neutrosophic sets**

**3.1 Definition:**

Let X be a set that is non-empty. The truth membership function TA (x), the contradiction membership function CA (x), an ignorance membership function KA(x), a unknown membership function along with a falsity membership function like that x X, and

When X is discrete. A is expressed as

A =.

**3.2 Definition**

The complement of an FPSVNS stands for and is written as,

**3.3 Definition**

The union of two FPSVNS A and B is stand for and it can be expressed as

**3.4 Definition;**

The intersection of two FPSVNS A and B and it is expressed as,

**3.5 Definition:**

Let X be a space that contains points (an object), where x represents a common element. A truth membership function TA (x), an indeterminacy membership function IA (x), and a falsity function FA (x) define an INS interval neutrosophic set A in X. There exists, for every point x in X,

and

. Thus, an INS A can be described as

x X}

={

Then the conditions can be met by the sum of. . Generally, an INS reduces to the SVNS when the interval values of TA (x), IA (x), and FA (x) are equal upper and lower ends. However, all the positions of neutrosophic sets are SVNSs and INSs.

**3.6. Definition**

The complement of an INS A is stand for and it can be expressed as

, and for any x in X.

**3.7. Definition**

An INS A is contained in another INS B, AB if and only if and .

**3.8. Definition**

If AB and B then two INSs A and B are equal, which is represented by the symbol A = B

**3.8. Definition: Correlation coefficient of QSVNSs**

As shown below, Rajashi Chatterjee [4] presented the idea of correlation coefficient of QSVNSs based on the correlation coefficient of SVNSs:

K (A, B) =

= --------- (1)

Following are the requirements for the correlation coefficient K (A, B).

1. K(A,B) = K(B,A);
2. 0
3. K (A, B) = 1, iff A = B.

There are some drawbacks to Equation (1), which are outlined below.

In the case of two QSVNSs A and B, if and /or

at all in X (i=1,2,3,…n).

Equation (1) is either undefined or not important. The formula given is not applicable here which is given in

Equation (1). Equation (1) only satisfies the necessary condition of the property (3), not a sufficient condition.

That is AB. Equation (1) may have the value 1.

**3.9. Example**

Let's take into account A and B as QSVNSs in X that are selected by and

. Here seemingly, AB.

Then K (A, B) = = 1\_\_\_\_\_\_\_\_\_\_\_ (2)

Therefore, it is not practical to use real-world examples of problems in this situation. So, we will define a better correlation coefficient as address these types of drawbacks.

**4. Improved to Correlation Coefficients**

The strengthened correlation coefficient of FPSVNSs has been defined in the next subsection using the correlation coefficient of FPSVNSs.

**4.1. Definition**

To determine the improved correlation coefficient between A and B, let us assume they are two FPSVNSs in the universe of discussion. X = {

M (A, B) = …..(3)

Where , , ,

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For any and i =1, 2, 3….n.

**Theorem 4.2**

For every two FPSVNSs A and B in the universe of discourse, X = {, the improved correlation coefficient M (A, B) satisfies the requirements mentioned below**.**

1. M(A,B) = M(B,A);
2. ;
3. .

PROOF:

1. It is obvious and forthright.
2. Here ,,,,

,,,,

. Consequently, the following in equation delight

Therefore, we obtain .

1. If M (A, B) = 1, next we obtain, =5. Since,,,

,, there are =1. And also since,,,

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We get and. This implies, ,

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Accordingly,, , , ,

for any , and i = 1,2,3,….n.

So A = B. ,

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Now in case that A= B, implies

, , , ,

for any, and i = 1,2,3,….n.

, ,,

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So we obtain M (A, B) = 1.

When we choose any constant in the following terms, the improved correlation coefficient formula that is given in (3) is valid and also meets the three criteria in Theorem 3.1.

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Let's think about the same situation in the example 2.12. when AB. M (A, B) = 0.912 can be found by using Equation (3).

**Example 4.3.**

Give us two FPSVNSs in X, and . Then it is clear that equation (1) is determined. So we obtain M (A, B) = 0.912 by applying equation (3). It convention that the drawback of the correlation coefficient in [10] is appropriately by the improved correlation coefficient as exposed above.

As a result, we generate a weighted correlation coefficient between FPSVNSs and take into account the differences in the elements. By choosing w i to be the weight for each element in X (i = 1, 2, 3... n), The weighted correlation coefficient between FPSVNSs A and B will be calculated. Next, the weighted correlation coefficient between the FPSVNSs A and B is calculated using the parameters &.

..(4)

If, Equation (4) becomes equation (3) at that point. The three terms in Theorem 3.1 are also satisfied by .

**Theorem 4.4**

The weighted correlation coefficient between the FPSVNSs A and B, represented by, is expressed by (4) and fits the requirements mentioned below. Let be the weight for each in X (i=1,2,3,…n), and .

1. ;
2. ;
3. . Theorem 3.1's attributes can be demonstrated similarly.

**4.5**. **Decision making method using the improved correlation coefficient of FPSVNSs**.

A multiple criteria decision making (MCDM) difficulty is when making decisions in a situation where numerous attributes are present. Before purchasing a vehicle, for example, one can look at the features that are offered in terms of pricing, style, safety, comfort, etc. In the context of a multiple attribute decision-making problem with Feramatean pentapartitioned single valued neutrosophic information, the following FPSVNS depicts the characteristic of an alternative Ai, (i =1,2,3,...m) on an attribute C j, (j=1,2,3....n).

….. (5)

Where and

, for

and i =1, 2, 3….m.

In order to make things simple, we will discuss the following five functions in terms of a fermatean pentapartitioned single valued neutrosophic value (FPSVNV): . Here, the expert or decision maker will typically determine the values of by evaluating an alternative, in relation to a criterion,. Due to this, we were given the fermatean pentapartitioned single valued neutrosophic decision matrix

D =.

An ideal FPSVNV can be described by dj in the case of perfect alternative A\*.In the decision-making process,

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In the case of perfect alternative an ideal FPSVNV can be expressed by

in the decision making method.

Hence the weight correlation coefficient between an alternative and the ideal alternative is given by, ..(6)

Where , , ,

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, , ,

, for I = 1,2,….m and j = 1,2,…n

We can determine the ranking order of all alternatives and pick the best one out of them by utilizing the weighted correlation coefficient (i=1, 2…m) mentioned earlier.

1. **Interval Fermatean Pentapartitioned Neutrosophic sets (IFPNS)**

**Definition 5.1**

An IFPNS A in x is represented by a truth membership function, a contradiction membership function, an ignorance membership function , an unknown membership function and a falsity membership function. For each point x in X, there are

and

. Consequently, an IFPNS can be defined as

x X}

={/ x X}

Next the sum of fulfill the requirements,

.

IFPNS decreases to FPSVNS if the lower and higher interval values of are equal. The branches of Fermatean pentapartitioned neutrosophic sets (FPNS) are IFPNS and FPSVNS.

**Definition 5.2** The complement of an IFPNS A is certified as and stands for

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For every x in X.

**Definition 5.3.** The other IFPNS B contains an IFPNS A, iff.

for each x in X.

**Definition 5.4**

If and, then two IFPNS A and B are equivalent, or A = B**.**

5.5. **Correlation coefficient between IFPNSs**. As an observation of the improved correlation coefficient of FPSVNSs, we have created an IFPNS-to-IPFNS correlation coefficient in this section.

**Definition 5.6.** In the discourse universe,, the correlation coefficient between two IFPNS A and B is represented as follows:

N (A, B) = { …..(7)

Where , ,

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Here, we suggest a weighted correlation coefficient between IFPNSs A and B by accounting for the weight of each element ( i = 1,2,…n) for each and i = 1, 2,…n.

Let be the weight for each element of (i=1, 2…n), and, then the weighted correlation coefficient between the IFPNSs A and B, which stands for , is represented by the following equation (8).

…….(8)

If , then equation (8) becomes like to equation (7). When

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in the IFPNS A and ,

, ,

, in the IFPNS B for any in X

The IFPNS A and B then become the FPSVNSs A and B, respectively, and equations (7) and (8) become equations (3) and (4) when i = 1, 2... n. In addition, N (A, B) and both meet the three requirements of theorems 3.1 and 3.2.

**Theorem 5.7**. The correlation coefficient N (A, B) for any two IFPNSs A and B in the discourse universe

, fits the requirements given below.

1. N(A,B) = N(B,A);
2. ;
3. .

It is also possible to show the properties of Theorem 3.1.

**Theorem 5.8**

The weighted correlation coefficient between the IFPNSs A and B, which is denoted by, and is expressed in equation (8) also satisfies the criteria specified below. Let be the weight for each element

and.

1. ;
2. ;

Theorem 3.1's attributes can be demonstrated in a similar way

.**5.9. Decision making method using the improved correlation coefficient of IFPNSs.**

In this instance, the following IFPNS represents the characteristic of an alternative on an attribute on a multiple choice making issue using interval Fermatean pentapartitioned neutrosophic information.

Where and

for and I = 1,2,….m.

Let's examine the following five functions for the sake of convenience.

, ,

, ,

, based on an interval fermatean pentapartitioned neutrosophic value (IFPNV)

The decision maker or wizard in this case normally determines the values of by evaluating an alternative in light of a criterion As a result, is an interval Fermatean pentapartitioned neutrosophic decision maker. Here, an ideal IFPNV is one that:

Applying equation (8) yields the weighted correlation coefficient between an alternative and the ideal alternative A\*.

= …..(9)

Where , ,

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For i =1, 2…m and j = 1, 2, 3….n.

The best choice can be selected after all the options have been ranked using the weighted correlation

coefficient .

1. **Illustrative example**

In this section, a multiple attribute decision-making dilemma is illustrated using an alternative that complies with the rules set forth in the fermatean pentapartitioned single valued neutrosophic environment and the interval fermatean pentapartitioned neutrosophic environment.

**6.1. Decision making under feramatean pentapartitioned single valued neutrosophic environment**.

The high-phone example that will be discussed in this location is about quality mobile devices with all applicable options set up various testing. The mobile1, mobile2, and mobile3 are each independently designated by the options A1, A2, A3 . The customer must reach a decision based on the following four criteria, specifically: (1) C1 is the cost; (2) C2 is the average scope. (1) C4 is the looks, (3) C3 is the character of the camera. According to the characteristics described in this sentence, we will draw the conclusion that the client will choose the best candidate according to the stabled order of all choices. The weight vector for the aforementioned characteristics is probably given by  . Here, the chances for evaluation will be evaluated in accordance with the five FPSVNS qualities listed above.

A rule expert will often evaluate an alternative Ai in relation to an attribute C j , (i = 1,2,3; j = 1,2,3,4,5) for each question. To be more exact, when asking someone their opinion on an alternative A1 in relation to an attribute C1, the likelihood that they will say the proposition is true is 0.5, that they will say it is both true and false is 0.4, that they will say it is neither true nor false is 0.3, and that they will say it is false is 0.2.

It may have been intended to read d11=〈0.5, 0.4, 0.3, 0.2〉 in the neutrosophic documentation. The following fermatean pentapartitioned single valued neutrosophic decision model will be obtained by repeating this approach for all three alternate about four characteristics.

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| --- | --- | --- | --- | --- |
| / |  |  |  |  |
|  | [ | [ | [ | [ |
|  | [ | [ | [ | [ |
|  | [ | [ | [ | [ |

Next, we will get the cutest alternative by applying the suggested strategy. Equation (6) can be used to determine the correlation coefficient.

,,

As a result, the ranking is. The most advantageous option out of the three is alternative (Mobile 1).

**6.3. Decision making under interval Fermatean pentapartitioned nuetrosophic environment.**

Consider the current similar model, where the four qualities are to be evaluated using IFPNSs to rank the three attainable options. Each fermatean pentapartitioned of a rule expert will complete the assessment of an alternative Ai regarding an attribute Cj (i=1,2,3;j=1,2,3,4) . The resulting interval fermatean pentapartitioned nuetrosophic decision matrix M is thus captured.

The best option will then be obtained by applying the suggested procedure. Equation (9) allows us to obtain the values of the correlation coefficient.

Hence ,, As a result, the ranking is . With accordance to the specified requirements in an environment with interval fermatean pentapartitioning, alternative (Mobile 2) is the best option out of the three.

1. **Conclusion**

We have defined the improved correlation coefficient of FPSVNSs, or IFPNSs, and we have also explored its aspects where the correlation coefficient of FPSVNSs defined in [] is confusing or nonsensical. Making decisions is a process that is necessary for dealing with problems in daily life. The two main steps in the decision-making process are determining the problem (or opportunity) and deciding to take action. Particularly, multiple attribute choice issues with several possibilities based on various criteria are probably an informative example. In this work, we investigated the pattern of decision-making using the elevated correlation between FPSVNSs and IFPNSs. Therefore, our anticipated increased correlation coefficient of FPSVNss and IFPNSs aids in labeling the most appropriate alternative to the client and likely.

**References**

1. D.A Chiang and N.P. Lin. Corrleation of fuzzy sets, fuzzy sets and systems 102 (1999), 221-226.
2. Mohana.K, Chiristy V, F.Smarandache, On Multi-criteria decision Making problem via Bipolar single valued neutrosophic settings, Neutrosophic sets and Systems 25(2019)125-135.
3. K Mohana, M Mohanasundari, Improved Correlation Coefficients of Quadripartitoned single valued neutrosophic sets and interval quadripartitioned neutrosophic sets for multiple attribute decision making 10.4018/978-1-7998-2555-5.ch014 (2020)
4. Rajashi Chatterjee, P majundar and S.K. Samanta, on some similarity measures and entropy on quadripartitioned single valued neeutrosophic sets, Journal of intelligent and Fuzzy Systems 30, 2016, 2475-2485.

5. F. Smarandache, A Unifying field in Logics, Neutrosophic Probability, Set and logic, American Reseach Press, Rcholoth,1999

6. Wang H. Smarandache F, Zhang Y Q, Sunderraman R (2010) single valued neutrosophic sets Multspace multistruct 4-410-113.

7. G.W.Wei,H.J.Wang and R. Lin, Application of correlation coefficient of Interval-valued intuitionistic fuzzy multiple attribute decision making with incomplete weight I formation. Knowledge and Information Systems 26 (2011), 337-349.

8. J.Ye, Multicriteria fuzzy decisision-making method using entropy weights-based correlation coefficients of interval valued intuitionistic fuzzy sets, applied mathematical Modeling 34 (2010), 3864-3870.

9. Jun Ye, Another form of correlation Coefficient between single valued neutrosophic sets and its multiple attribute decision Making Method, Neutrosophic Sets and Systems, 1,8-12.doi.org/10.5281/zenodo.571265

10. J.Ye.Multicriteria decision making method using the correlation coefficient under single valued neutrosophic environment, International of general Systems 42(4) (2013), 386-394.

11. Jun Ye and Qiansheng Zhang(2014), Single valued Neutrosophic Similarity Measures for Multiple attribute decision making Neutrosophic Sets and Systems, 2.48-54.doi.org/10.5281/zenodo.571756

12. Jun Ye, Florentin smarandache (2016), Similarity Measure of refined single valued Neutrosophic Sets and its multicriteria Decision making method, Neutrosophic sets and Systems, 12,41-44.doi.org/10.5281/zenodo.571146

13. J Ye. Correlation coefficient of dual hesitant fuzzy sets and its application to multiple attribute decision making, Applied mathematical Modeling 38 (2014), 659-666.

14. J.Ye. Improved correlation coefficients single valued neutrosophic sets and interval neutrosophic sets for multiple attribute decision making. Journal of intelligent and Fuzzy Systems 27 (2014) 2453-2462.

15. Subha R., K.Mohana (2023), Fermatean pentapartitioned nuetrosophic sets, Indain Journal of Natural Sciences, vol.14/Issue 77/April/2023, international Bimonthly (Print) – Open Access. ISSN:0976-0997