Triaxial Star

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**Abstract:** The idea of a “Triaxial Star” first proposed by Chandrasekhar in 1969. More than 50 years passed, the detection of triaxial star remains unreachable. Detection of gravitational waves would be a probe to the astronomers to investigate the properties of the compact objects in a new direction in the light of gravitational waves. Recent discovery of cosmic baby , i.e., swift J1818.0-1607 with age ~ 300 years, offers the astronomers an opportunity , through continuous observations, to increase our knowledge about the physics of the evolution of a magnetar from its new born phase to end stage, generation of ultra-strong magnetic field in its interior, source of continuous gravitational waves, physics of coupling between magnetic field decay and cooling for keeping the internal temperature ~ 108 K for a period of ~ 104 years, , etc. Cosmic Baby most probably the first detected Triaxial star.

**Key Words:** Ellipsoid, Triaxial Star, Gravitational Waves, Neutron Star, Magnetar

**Content**

1. Introduction: Compact Star and Professor Chandrasekhar
2. What is Triaxiality in a Star
3. General Properties of Equilibrium Figure

3.1 Triaxiality and Gravitational Waves

1. Deformation of a star due strong magnetic field
2. The Ellipticity of a Star

Surface Ellipticity,

Quadruple Ellipticity

1. Magnetar and Triaxiality
2. Recently detected Magnetar, the Cosmic Baby
3. Ellipticity of the Cosmic Baby Magnetar Swift J1818.0-1607
4. Origin and decay of core magnetic field of Swift J1818.0-1607

1. Ellipticity and Triaxiality of Swift J1818.0-1607

Rotational vs Magnetic Energies

Estimation of the triaxiality of Cosmic Baby

1. Conclusion: What do we want from Triaxial Cosmic Baby
2. **Introduction: Compact Star and Professor Chandrasekhar**

A compact star is a system inside which a struggle is continuing between gravity and degenerate pressure created by its constituents. Gravity tries to crash the star’s material by pulling towards the center of star, while degenerate pressure, created among the material particles due compactness, tries to counteract and overcome the gravity pull. In his book “An Introduction to the study of Stellar structure (Dover, 1967)“ Professor Chandrasekhar first gave a detailed picture of “what is a star, what is going on inside it, etc” in the form of mathematical language.

Before the discovery of neutrons in 1932, electrons were the latest discovered particles on that time. Professor Chandrasekhar thus considered the latest star, i.e., white dwarf. He calculated the maximum mass of a white dwarf full of electrons = 1.4 M⊙ ( M⊙ being the solar mass) which is known as Chandrasekhar limit. In 1932 Chadwick discovered neutrons. Then T. Gold proposed the possible existence of a new compact star beyond white dwarf, called Neutron Star which is made full of neutrons.

In the year 1969 Professor Chandrasekhar theoretically proposed another new compact star, called “Triaxial Star”. Note that, in 1967 Jocelyn Bell, a Ph.D. scholar of Cambridge University, UK, detected a peculiar type signal but its rhythm was very accurate. This star later identified as neutron star. However, the triaxial star was confined in theoretical works only although neutron stars ( isolated , rotating neutron stars or pulsars, and magnetars) became a gold mine to the astronomers and scientists. In searching the gravitational wave sources, isolated neutron stars, millisecond pulsars became the efficient gravitational wave sources. Many theoretical studies suggested that the triaxial neutron stars, i.e. triaxially deformed neutron stars, are the most significant gravitational wave sources . So, triaxially deformation in star thus gave an impetus to the astronomers, scientists to search for a triaxial star.

1. **What is Triaxiality in a Star**

More than 50 years passed after the proposed concept of triaxial star but till date it is remained undetectable. Several theoretical works suggested that star with fast rotation can be deformed and would become a triaxial star . Classically, the figures of equilibrium of uniformly, rotating homogeneous masses pertain various sequences of ellipsoidal figures. The Maclaurin sequence is a sequence of oblate *spheroid*s along which the eccentricity (“e” ) of the meridional sections *increases from zero to one* (Chandrasekhar and Lebovitz 1964 ). Initially it was though that the sequence of the square of the angular velocity of rotation ( Ω2) is not a parameter of unrestricted range. This means that for each value of Ω2 , (except less than a certain determinate maximum, there are two permissible spheroidal figures of equilibrium. But Jacobi first showed that a sequence of genuine triaxial ellipsoids of equilibrium diverges from the Maclaurin sequence. This means that there is a bifurcation point which clearly distinguish the permissible sequences of figures of equilibrium from Maclaurin spheroidal sequence to Jacobi ellipsoidal sequence.

Let us consider a situation of general ellipsoid ( also called a triaxial ellipsoid, see fig.1) whose quadratic surface can be expressed in Cartesian co-ordinates by

( x2/ a2 ) + (y2 / b2) + (z2 / c2) = 1 (1)

where the semi – axes are of lengths a, b, c.

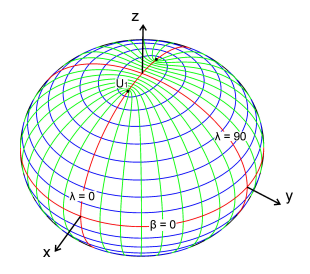
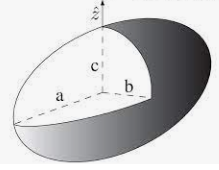
Now,

1. If all the three are same, i.e., a = b = c then it is a sphere.
2. If the length of two axes of an ellipsoid are the same, then the figure is called a spheroid , i.e., an oblate spheroid or a prolate spheroid depending on whether c < a or c > a, respectively.

In spherical coordinate system (r, θ, ϕ ) the eqn. (1) becomes

 (2)

Geodesic form

 (a)  
 (b)

**Fig. 1 :** (a) Ellipsoid in Cartesian Coordinates (b) Ellipsoid in Geodesic Coordinates (Panou 2013)

In this case we consider a triaxial ellipsoid where Cartesian coordinates are ( x, y, z ) but three semi-axes are a = ax, b = ay, and c = b then eqn.(1) takes the form

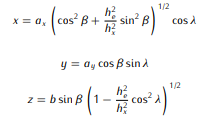
 (3)

The linear eccentricities can be calculated as

 (4)

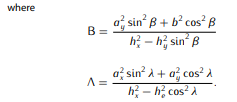
and he2  = hx2 – hy2 .

This triaxial ellipsoid can be parameterized as

 (5)

where  Ellipsoidal latitude and ellipsoidal longitude can therefore be interpreted with the help of this parameter. Thus, in this parameterization the first fundamental coefficients E, F, G can be expressed as (Panou 2013)

 (6)

 (7)

This implies that

1. F = 0 indicates that the β-curves and λ-curves are orthogonal.
2. B 0 and Λ 0 for all points and E = G = 0 means umbrella shape.
3. For an orthogonal parameterization the line element “ds” on the triaxial ellipsoid is

ds2 = E dβ2 + G dλ2 (8)

1. **General Properties of Equilibrium Figure**

A relative equilibrium figures concern, in general, the liquid figures such that an equatorial symmetry plane exists. It has a similar situation in the case galaxies. This means that for liquid and stellar figures the internal flows are absent. Naturally, it is believed that for all figures of

equilibrium figures a much stranger inequality is present, namely, angular velocity Ω2 / ( G) 0.45 satisfying the validity of Maclaurin spheroid.

Now, we can consider rotation in equilibrium figure. In that case, the liquid figures of relative equilibrium can rotate only around the least axis. In triaxial liquid figure, i.e., with internal flow, can rotate around the middle axis and possess an oblique rotation. In stellar system this equilibrium figures can rotate around any of the three axes turn into so called “interia ellipsoid” or “inclined rotation”. Although there is no direct relation between an angular velocity and flattening for equilibrium figures of relative equilibrium but direction of internal flows w.r.t. rotation of the figure plays an important role in astrophysics for modeling of stars and galaxies where consideration of complex interrelation (i.e., anisotropy) is essential.

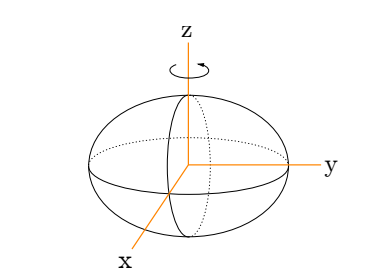
As all the gravitating equilibrium figures are of negative heat capacity, an interpretation of bifurcation point, creates an interest for astrophysical degenerate systems or compact objects. The ratio of rotational kinetic energy (T) and gravitational binding / potential energy (W) , i.e., T/ |W| therefore indicates whether the system with the angular momentum distribution for axisymmetric ( i.e., for Maclaurin spheroid) or non-axisymmetric (Jacobian ellipsoid). We know that a stable star can be deformed if it rotates faster. Rapid rotation in a star (i.e, for self-gravitating, incompressible fluids in equilibrium) differentiates its new figure from the earlier one i.e.,

1. Figure of axisymmetric Macllaurin spheroid (earlier) ;
2. Figure of non-axisymmetric, i.e., Triaxial Jacobi ellipsoids (new figure)

when the ratio of T/ |W| reaches ~ 0.14 (Bonazzola et al 1998). We can say, this new configuration is no longer a precise ellipsoid in relativistic gravity or for compressible fluids, it is a triaxially deformed rotating compact star ( or simply “Triaxial Star” ) rather than ellipsoids. Question is —why triaxial figure is important ? The simple answer is : In relativistic astrophysics with the help of triaxiality it is possible to accommodate fluid compressibility for modeling the relativistic neutron star as an axisymmetric and uniformly rotating configuration associated with the equation of state (EoS) of high density nuclear matter.

**3.1 Triaxiality and Gravitational Wave**

Let us consider a triaxial configuration having tri-planar symmetry w.r.t. three orthogonal X, Y, Z planes for relatively stiff (piecewise) polytropic equation of state. In this case, the possible situation is the masses, obtained from supra-massive triaxial solution, exceed the maximum mass of the spherical solution but are always lower than those of axisymmetric equilibrium. Under this situation two facts are very important :



**Fig. 3:** : Diagram of a rotating triaxial ellipsoid, with its major axes aligned to a

rectangular coordinate system, spinning about the z axis (Neunzert 2019)

1. The difference in the maximum masses of triaxial star and axisymmetric equilibrium solutions depends on the equation of state (EoS) ;
2. If this difference turns out to be only 10% , then it will indicate a strong evidence of substantially softer EoS of high density matter in the core of a neutron star.

Another important situation we have to consider for a newly born neutron star which is supernova fall back accretion and condition for gravitational collapse. We now consider a situation. We know that a neutron star is born from supernova with a strong magnetic field (B) 5 x 1014 G and rotates as fast as T/ |W| ~ 0.14 for 50 – 200 s until the star collapses to black hole. This possible situation is nothing but a triaxially deformed compact star that may be formed triaxially from massive stellar core collapse. If this happens, i.e., once such triaxial star is formed, enormous amount of gravitational waves would be emitted. This provides us an opportunity to extract properties of high density nuclear matter situated in the interior of a compact star like neutron star. For example, the typical values of the amplitude (h) of gravitational waves produced from a triaxial star can be estimated using the relation:

h ~ 9.1 x 10-21 (30 Mpc / D ) ( M / 1.4 Mo )3/4  ( R / 10Km )1/4  - 1/5  (9)

where D, M, R and f are the distance to source, the source mass, the mean radius, and the wave frequency in Hz , respectively. Piro and Thrane ( 2012) estimated the detectability of gravitational waves produced by triaxially compact stars under the fall back accretion scenario for Advanced LIGO detector (Harry 2010) ~ 17 Mpc.

1. **Deformation of a star due strong magnetic fields**

Theoretical models of neutron stars, in general assumed that they are made entirely of neutrons. In general relativity, the equilibrium configuration of neutron star (i.e. by solving Einstein-Maxwell equations) is coupled with both rotation and magnetic field i.e., consideration of magnetic field is essential. This means in a spherical symmetric back ground perturbation due to internal magnetic field in the shape of neutron star surface structure would appear. Therefore, a neutron star or magnetar (the special type of neutron star with internal strong magnetic field) can significantly be deformed by both rotation and strong magnetic field. Theoretical calculation (Bonanno et al 2003) hints that at the end of the collapse of the core of a massive star, differential rotation could generate a strong toroidal magnetic fields ~1016 – 1017 G inside the proto-neutron star. Of course, the relativistic models of magnetized stars (i.e., neutron stars, magnetars) require the simultaneous of both poloidal and toroidal field components. The combined effects of magnetic field and rotation could make:

1. An apparent change in shape (i.e. surface deformation) which is relevant for the electromagnetic emission, and also
2. On the internal matter distribution (i.e. the quadruple distortion) that is relevant for the emission of gravitational waves.
3. **The Ellipticity of the Star**

The stellar deformation can be expressed in terms of stellar ellipticity or simply “ellipticity”(ϵ ). There are two definitions relevant for two conceptually different quantities — i) the surface ellipticity (ϵsurface) and ii) the quadruple elliptcity (ϵqud ).

1. The Surface Ellipticity

The surface ellipticity can be defined as (Chandrasekhar and Miller 1974)

ϵsurface = ( Equatorial radius Re  - ( Polar radius Rp ) / (Polar radius Rp ) (10)

In the case of neutron star, to know the degree of deformation we can write

ϵ = 1 – ( Rp / Re )2 } (11)

The equ.(1) describes the geometrical shape of the star. This means the surface ellipticity describes the external appearance of the star.

In case of neutron star, the above equ. (2) gives us a relationship between the mass and radius of the neutron star. The known facts are :

1. If the polar radius Rp of the neutron star increases, then it’s mass decreases.
2. If the equatorial radius Re of the neutron star increases, the mass increases.
3. The maximum deformation appears at the ellipticity ϵ ~ 0.257. In this case Re > Rp such that the neutron stars are maximally in oblate form.
4. The Quadruple Ellipticity

It is a measure of the mass quadruple of the star (Bonazzola and Gourgouljan 1996, Haskell et al 2007) which can be expressed as

ϵQuad = - Q / I (12)

where I = the mean value of the moment of inertia of the star, and Q = its mass – energy quadruple moment.

This quadruple ellipticity can also be written in terms of inertia components:

ϵQuad = ( Izz – Iyy ) / Izz (13)

In general, the quadruple ellipticity is a measure of the entire stellar balk deformation. It is used to evaluate the gravitational wave emission of a rotating neutron star.

1. **Magnetar and Triaxiality**

A magnetar is a neutron star with an ultra-strong magnetic field. At ~1015 G which is thousand trillion times stronger than the Earth’s, and between 100 and 1,000 times stronger than that of a radio pulsar, making them the most magnetic objects known.

Like other neutron stars, magnetars are around 20 kilometres in diameter, and have a mass of about 1.4 M⊙ . They are formed by the collapse of a star with a mass 10–25 M⊙. They are different from other neutron stars by having even stronger magnetic fields, and by rotating more slowly in comparison. Most observed magnetars rotate once every 2 – 12 s (Kaspi 2010 ) , whereas typical neutron stars, observed as radio pulsars, rotate one to ten times per second ( Condon and Ransom 2021). The important properties of a magnetar's magnetic field gives rise to very strong and characteristic bursts of X-rays and gamma rays. However, the active life of a magnetar is short compared to other celestial bodies. Their strong magnetic fields decay after about 10,000 years, after which activity and strong X-ray emission cease.

Regarding the formation of the magnetar it is believed that they are formed in the same way as all neutron stars, through the core-collapse of a massive star in a supernova explosion. It is not entirely clear what conditions cause a magnetar to be created instead of an ordinary neutron star or pulsar, but in order to achieve such strong magnetic fields, some theories suggest the neutron star must initially rotate between 100 and 1,000 times per second.

The dominant theory of the strong fields of magnetars is that it results from a magneto-hydrodynamic dynamo process in the turbulent, extremely dense conducting fluid that exists before the neutron star settles into its equilibrium configuration (Thompson and Duncan 1993). These fields then persist due to persistent currents in a proton-superconductor phase of matter that exists at an intermediate depth within the neutron star (where neutrons predominate by mass). A similar magnetohydrodynamic dynamo process produces even more intense transient fields during coalescence of pairs of neutron stars (Price and Rosswog 2006). But another theory is that they simply result from the collapse of stars with unusually strong magnetic fields( Zhou et al 2019).

Note that the measurement of the spin-down rate of a SGR from observed pulsations suggested that it was a neutron star with a magnetic field strength of 8 × 1014 G and since that time, both SGRs and anomalous X-ray pulsars have been explained successfully by the magnetar model which is based on the decay of the magnetic field powering the emission of X-rays and gamma rays. However, it appears that magnetars are only X-ray bright for a short period of time since their pulse periods are clustered between 6 and 12 seconds. If they remained active for an extended period of time, we should also see magnetars with pulse periods of tens of seconds or longer.

1. **Recently detected Magnetar, the Cosmic Baby**

On 12th March 2020 at 21:16:49 UT the Swift Burst Alert Telescope (BAT) on board the Neil Gehrels Swift Observatory ( Gehrels et al 2004 ) detected a typical characteristics of short burst from magnetar ( Evans et al 2020 ). 64 seconds afterwards observation by the Swift X-ray Telescope (XRT) finally detected a new uncatalogued x-ray source, so called Swift 1818.0 – 1607 which is presently known as Cosmic Baby. The important parameters of this cosmic baby , obtained from the timing analysis of early observations at the time of discovery, are shown in table I.

**Table I :** Various early observed / measured parameters of Swift J1818.0 – 1607 (Parui 2023,2023a)

|  |  |  |
| --- | --- | --- |
| Typical properties | Value | Reference |
| Characteristic age  (shortest known ) | ~ 240 years | Esposito et al (2020 ) |
| Surface magnetic field | ~ 2.7 x 1014 G |
| Dipolar magnetic field at poles | 7 x 1014 G |
| Spin down Luminosity ( Ėrot) | ~ 1.4 x 1036 erg.s-1 |
| Luminosity | ~ 8 x 1034 erg.s-1 |
| Coherent periodicity of x-ray signal | 1.36 s | Enoto et al (2020 ) |
| Spin period derivative | ~ 8.2 x 10-11 s.s-1 | Champion et al  (2020) |
| Period derivative | ~ 9 x 10-11 s.s-1 |
| Spin Period | 0.7333920 s |

After a series of observations through various telescopes (such as TMRT, NICER ) at several wavelengths till July 27, 2020 some confirmed parameters of the cosmic baby magnetars were available. For example: Rotation / spin period derivative is ~ 3.74 x 10-11 s-2, surface dipole magnetic field ~ 3 x 1014 G, spin down luminosity ~ 1.1 x 1036 erg. S-1, etc. Although Chandra Observatory ( Blumer and Safi-Harb 2020 ) began its observation to swift J1818.0 – 1607 less than a month after the discovery of cosmic baby but its observations gave the astronomers the first high resolution view of the cosmic baby in x-rays. Still there is a lot of variation almost in all parameters of the cosmic baby properties.

1. **Ellipticity of Cosmic Baby Magnetar Swift J1818.0-1607**

In order to explain the properties of transient sources of gamma ray i.e. Soft Gamma Repeaters (SGRs) the concept of Magnetar arose. The power (i.e. energy) from rotation is unable to explain the above fact. Thus, as an alternate, these peculiar high energy sources could be powered from the ultra-strong magnetic field. As the Magnetars are isolated young Neutron Stars having intense magnetic fields which power a wide variety of high energy-emission from giant flares to fast radio bursts, the basic idea regarding these peculiar high energy sources could be the ultra-strong magnetized neutron stars, magnetars with surface (dipole) fields in the range 1014 – 1016 G and internal magnetic fields >~1016 G ( at least one order of magnitude stronger ) (Paczynski 1992, Thompson and Duncan 1995 ). As the density of the neutron star core is beyond the density ~ 1015 g.cm-3, it creates an anisotropic nature of the compact object ( Ruderman 1972 ) i.e. internal pressure can be decomposed into two parts: the radial pressure (pr) and the transverse pressure (pt) where pt is the orthogonal to pr . This pressure anisotropy affects the physical properties, stability and structure of the stellar matter ( Dev and Gleiser 2002) . The ultra-strong internal magnetic field of the stellar matter can also create anisotropic pressure i.e. the deformation of spheroidal shape of rotating neutron star and emission from it due deformation.

Cutler ( 2002 ) first pointed out the internal field structure of a neutron star becoming an effective, efficient source of GW emission. According to him a magnetically distorted neutron star, i.e. a neutron star with a strong internal toroidal field, turn into a prolate shape that offer the best chance of being a strong GW emitter. Thus, the ellipticity of the magnetic deformation (**ϵ**) in the shape of stellar object has crucial role in the strong GW source. Precisely, the triaxiality of the stellar body —its dependence on the internal strong magnetic field strength, decay of the field strength, dynamical shape transition to a triaxial ellipsoid configuration.

A magnetar is a slowly rotating isolated neutron star having very strong internal magnetic field ranging 1016 – 1018 G and even more up to 1020 G ( Lai and Shapiro 1991). In general, a magnetar is a triaxial stellar body (Melatos 1999) , particularly in it’s new born phase. Its internal ultra-strong magnetic field (i.e. the toroidal magnetic field is greater than at least one order of its surface dipolar magnetic field) is estimated by inferring from the geometric distortion of the neutron star (or magnetar) caused by strong toroidal magnetic field. Therefore, limits on the ellipticities of magnetars can be used to constrain the toroidal magnetic field as a period or duration of GW emission. So, if the field is dipolar, then hydro-magnetic stresses, arising from non-radial gradients of the super-strong internal magnetic field, deform the magnetar (i.e. between the magnetic poles and the equator ) and the fractional difference (ε) between the principal moments of intertia can be expressed as ( Melatos 1999; Goldreich 1970; deCampli 1980)

ε ~ δp R5 / I1 2 x 10-9 (Bint / 1010 T )2 (14)

where δp = induced matter-density perturbation

~ Bint 2 / μoCs2 ,

R = the stellar radius,

Cs = the isothermal sound speed ( = 3-1/2 c, c being the velocity of light),

Bint = the characteristic magnitude of the internal magnetic field such that

1. ≈ Bo, if the internal magnetic field is confined to the stellar crust,
2. >~ Bo, if it is generated deep inside the star (i.e. convective dynamo model ( Thopson and Duncan 1993),
3. Bint <~ 109 T in the case of rotation powered pulsars

The significant characteristics if the triaxial star are (Melatos 1999) :

a) the hydrodynamic deformation in a magnetar is much larger in comparison to the elastic deformation arising from shear stresses in the crystalline stellar crust of a rotating neutron star;

b) the principal axes of inertia in a rotating neutron star are oriented arbitrarily w.r.t.the magnetic axis of the external magnetic dipole field.

It it to be noted that in the case of magnetar the magnetic axis is approximately parallel to one of the principal axes of inertia (say **e**3 ) i.e. the alignment of magnetic axis is not exact to inertia axis due to the complicated structure of the internal field near its generation site (i.e. in other word, a non-axisymmetry state remains).

1. **Origin and decay of core magnetic field of Swift J1818.0-1607**

Idealizing the magnetar as a neutron star with the shape of slightly deformed, homogeneous ellipsoid and having a small ellipticity

= ( I1 –I2 ) / I3 (15)

where I1, I2, I3 are the principal moments of inertia of the neutron star such that I3 is assumed to be aligned with the spin axis then using eqn. (10) we obtain the following constraint on the magnetar ellipticity (Moriya and Tauris 2016 ) as

| | < (5 / 3G )1/2 { C R3 Po Bdipole / 24 I } (16)

Using the standard neutron star properties of I=1045 g.cm2, R = 10 km, Po = initial spin period and the angle between the spin axis and the principal axis of the neutron star distortion = /2 ( Cutler and Jones 2001) equ. (16) turns into

| | 3 x 10 – 4 ( Bdipole  / 1014 G ) (Po / 1ms) (17 )

Now, under the assumption that magnetar’s internal toroidal magnetic field component (Btoroidal ) is the main cause of neutron star deformation then we can constrain the average value of this component by the relation (Cutler 2002 )

| | ~ 1.6 x 10 – 4  (Btoroidal  / 1016 G ) 2 (18),

and Btoroidal  as (Moriya 2016)

Btoroidal  < ~ 1.4 x 1016 G ( Bdipole / 1014 G) ½  (Po / 1 ms ) 1/2  (19)

Using the available parameters, such as observed dipolar magnetic field strength Bdipole = 7 x 1014 G , spin period Po = 1.36s of the Swift J1818.0-1607 we can estimate the ultra-strong internal toroidal field strength Btoroidal <~ 1018 G. This value is consistent with the value 1017 – 1018 G in the case of newly born proto-neutron stars (Del Zanna et al 2018; Ciolfi et al 2019; Franceschetti and Del Zanna 2020 ) and also supports the model proposed by Dall”Osso et al (2012) that the internal magnetic field must be a very large initial value ( >~ 1016 G) for the internal magnetic field decay.

*The decay of Core Magnetic field*

Theoritical Studies (Dall’Osso et al 2012; Thompson and Duncan 1996) of magnetic field decay in neutron star core hint three possible separate processes — ohmic dissipation, ambipolar diffusion and Hall drift are involved which affect the evolution and dissipation of magnetic fields in magnetar interior .In particular, ohmic dissipation and ambipolar diffusion are directly active in dissipation while Hall drift is active indirectly. Further studies (Goldreich and Reisenegger 1992; Pons and Geppert 2007) also indicate the conservation of total energy remains almost same after the Hall drift i.e. due to Hall diffusion a new equilibrium configuration with smaller total energy will appear in the magnetar interior. But initial stable magneto-hydrodynamic configurations remain close to the new equilibrium configuration as per results found in their studies. Even, the ambipolar diffusion in the neutron star core is expected to be dominant mode of interior field decay as long as early phase evolution ( i.e. ages much less than ~104 yrs) of magnetar is concerned.

However, it is suggested that the ambipolar diffusion (Goldreich and Reisenegger 1992; Pons and Geppert 2007) at high temperature in neutron star ( i.e. magnetar) core has a leading role. As the neutron star (i.e. magnetar) core magnetic field <~ 1018 G (which is >~ 1016G) the temperature in the magnetar core material will be > 109 K. In this case the field decay is not frozen. This means an equilibrium condition between heating and cooling in the high-Temperature regime may appear. This means that magnetar core fields larger than that would be able to

1. dissipate enough energy as well as
2. to balance neutrino cooling in the early phase under the effective solenoidal and irrotational modes are still degenerate.

It can be said that the field decay is negligible as long as the temperature is high enough ( e.g. > T9 ) when the time scale of field decay occurs on the same time scale in both two modes. The significance of ambipolar diffusion is that

1. it becomes active soon after the formation of magnetar , and
2. it can prevent the cooling of magnetar core below a temperature ~ 109 K for a period of thousands yrs ( at least 103 yrs ) ( Zhou et al 2018).
3. Coupling of heating and cooling — the decay of an internal magnetic field >~ 1016 G couples with the magnetar cooling at the early stage.
4. **Ellipticity and Triaxiality of Swift J1818.0-1607**

*Rotational vs Magnetic Energies*

It is believed that a newly born rotating compact star can also achieve higher value of T / |W| when it is born from core collapse supernova. In that case, for a triaxial neutron star, the ratio T / |W| is essentially constant along with the triaxial sequence for higher compactness (Zhou et al 2018 ).

Till date thirty magnetars have been discovered excluding this swift J1818.0-1607. For these 30 magnetars their spin / rotational periods range 2 – 10 s and surface dipolar fields (calculated from the periods, period derivatives ) are 1013 – 1015 G (Kouveliotou et al 1999) . But study (Jawor and Tauris, 2022) showed that initial period of magnetar must be less than 2s. Analysis of observed data indicates magnetars are young and most of them having characteristic spin down ages of less than 104 years (White etal 2022). Since they are slow rotator, so spin down energy losses can not power their emission. Here**, a significant finding is that the rotational effect is negligible for the magnetar** (Kiuchi et al 2011). As a result, magnetic induced deformation is an alternate for obtaining the triaxial sequence.

Alternate source is believed to be the dissipation and re-arrangement of their magnetic energy. Magnetar interior structure specially equation of state (EoS) and the cooling process in the simultaneous presence of high density, strong gravity, and strong magnetic field is important in determining the deformation in shape as well as triaxial value of the magnetar ( Yakovlev et al 2005; Chamel and Haensel 2005).

Numerical simulations (Lindblom et al 1998; Doneva et al 2015) showed that a newly born magnetar will born with a strong magnetic field and a rapid rotation which lead to the stellar deformation. As a result a magnetar can emit observable gravitational waves i.e. a baby magnetar will spin down due to a magnetic dipole torque as well as gravitational wave quadrupole radiation. Spin down evolution of the magnetar also produces electro-magnetic radiation. In other words, the dynamic evolution of magnetar spin down provides a relation to the theoretical breaking index (n) such that

1. n = 3 when magnetic dipole radiation (i.e. electromagnetic phenomena ) dominates the spin down of the magnetar ;
2. n = 5 when the GW radiation dominates the magnetar spin down.

The comparison between the observed spin down light curves and their related models provides us an opportunity to constrain the initial spin period (Po), dipole magnetic fields (Bdipole) and the ellipticity ( ) of the neutron star (i.e. magnetar). For example, magnetars with initial period Po ~ 1 ms and surface dipole magnetic field Bdipole ~ 1014 – 1015 G usually have the ellipticity ~ 10 -3 . But theoretical value of the minimum rotation period of the magnetar is ~ 0.3 – 0.5 ms ( Koranda et al 1997) . The best fitting relations (Xie et al 2022) are

log = 3.79+0.52-0.43  + ( 2.19 +0.17-0.15 ) log Po (20)

and log = - 22.50+2.15-2.22 + (1.29 +0.15-0.14 ) log Bdipole (21)

suggest that

1. magmetar having a stronger magnetic field and / a slower spin period corresponds to the longer ellipticity;
2. a longer rotation period corresponds to possession of a stronger magnetic field;
3. the neutron star deformation is related to its surface dipole magnetic field to some extent.

But it is argued (Majid et al 2022; Rizaldy et al 2018 ) instead of dipole magnetic field neutron star deformation may be induced by a strong internal magnetic field (Bint ) in the stellar core through the relation

10 – 8  (Bint / 1012 G) (22)

This relation hints the possession of a very strong internal magnetic field (i.e. Bint ~ 1016 – 1017 G) is needed in order to obtain the ellipticity ~ 10 – 3 – 10 – 4  and also the required strength of the internal core magnetic field which should be at least 1 – 2 order of magnitude greater than the surface (i.e. external ) magnetic field ( Bdipole  ~ 1015 G ).

***The Estimation of the Triaxiality of Swift J1818.0-1607***

We can estimate the triaxiality of cosmic baby by using the relation in equ. (22) with the observed parameter at the time of its discovery on 12th March 2020 :

i.e. rotational period = 1.36 s, surface dipolar magnetic field = 3 x 1014 G, surface magnetic field at poles = 7 x 1014 G, characteristic age ~ 300 years

Using equations (17), (18), (19) and (22) and with the above parameters as input we calculate **the ellipticity, internal core magnetic field of Swift J1818.0-1607 and found ~ 9 x 10 -3 and 8.9424 x 10 17 G, respectively**.

It is noteworthy that Numerical Simulation study (Rizaldy and Sulaksono 2018) of magnetized deformation of neutron stars shows an interesting consequence for neutron stars with low masses i.e. the effect of magnetic field is more prominent for internal magnetic field Bint > 4 x 10 18 G. According to Rizaldy and Sulakseno (2018) the balance between the gravity and magnetic field is significantly different for different directions in the case of small mass rather than massive neutron star. Even the gravity pull of magnetic field on the z-axis is significantly more than for the other axes resulting which oblate-shape appears in the low mass neutron stars. In the case of massive neutron star this oblate shape is very less in comparison to that of less massive. In other words, we can say internal toroidal magnetic field is more effective than the poloidal field. ***The deformation associated to the poloidal field ( Bp 1014 and 1015  G) and the corresponding correction in ellipticity (i.e. ~ 10 - 4 – 10 – 2 , respectively) is negligible*** ( Morasi et al 2011).

Although the recent view of magnetized deformation of neutron stars (i.e. magnetars ) is due to the effect of both the toroidal and the poloidal magnetic fields i.e. a mixed magnetic field . As the contribution of the poloidal field component in deformation is negligible we shall consider the effect of toroidal magnetic field only. Because our main purpose is to check the ellipticity of the deformed neutron star i.e. magnetar Swift 1818.0 – 1607 and its stability. In a comparative analysis pulsars and magnetars Heras (2012) found the initial magnetic fields in the interior of nascent neutron stars lie in the range 1014 – 1016 G in realistic case. As ambipolar is active that prevents both the decay of interior magnetic fields and cooling of the neutron star i.e. magnetar (as the effect is same and applicable for magnetars as well as neutron stars also ) such that magnetar core temperature stays higher than several times 108 K for a period of few thousands of years ( at least 103 years) . This ellipticity of new born magnetar might not be changed too much during the period of thousand years. As the characteristic age of the Swift J1818.0 – 1607 is only ~ 300 years i.e. the baby phase still compare to thousands years it will definitely exhibit triaxility i.e. triaxial behavior at least up to its age 1000 years.

The estimated ellipticity of this magnetar lies within the range for triaxiality and its ellipticity will remain on that value for exhibiting triaxial nature for several thousands years. Thus, we can consider the Swift J1818.0 – 1607 as a triaxial magnetar or simply a triaxial star.

1. **Conclusion : What do we want from Triaxial Cosmic Baby**

Newly born rotating neutron star can break their axial symmetry spontaneously if the ratio T / |W| exceeds some threshold value. Magnetars are classified as a rare class of relatively slow rotating neutron stars that possess very strong magnetic fields. As a non-dissipative mechanism a magnetic field with a component parallel to the rotation axis breaks circular conservation and introduces symmetry breaking spontaneously. The swift J1818.0-1607 is a baby magnetar of characteristic age of ~ 300 years, having very strong internal core magnetic field ~ 8.9424 x 1017G. It is the fastest among the detected 31 magnetars having spin or rotational period ~1.36 s. Its magnetic fields are not aligned with the rotational axes. The above properties of the swift J1818.0-1607 indicate that it is an ideal triaxial magnetar (compact object) where detection of a triaxial star and its bizarre properties can be tested / studied. Its internal core magnetic field, though too much strong, yet have ( at least) a slow decay mode through ambipolar diffusion which becomes active soon after formation (birth). As this process can prevent the cooling of the magnetar core below a temperature of few times of 108 K (i.e. < 109 K) for thousands of years, continuous observation of Swift J1818.0 – 1607 will thus offer us an opportunity for understanding our knowledge of the evolution of magnetic fields of magnetars.

Finally, one can conclude that Cosmic Baby is most probably the detected “**First Triaxial Star”**

As the rotational period of this magnetar is 1.36s i.e. within the range 1 – 10s, the frequency of the emitted continuous gravitational waves would be very low (Sieniawska and Bejger 2019; Ibrahim et al 2023 ) this author encourages the Gravitational Wave Community to observe this triaxial baby magnetar (i.e. the swift J1818.0-1607) continuously during their observation of compact objects through electromagnetic counterparts. It is hoped that future observed data definitely help us for better understanding the physics of the evolution of the Magnetars.

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